

1. convert $(86)_{10}$ into binary.

$$\begin{array}{r|l}
 2 & 86 \\
 \hline
 2 & 43 - 0 \\
 \hline
 2 & 21 - 1 \\
 \hline
 2 & 10 - 1 \\
 \hline
 2 & 5 - 0 \\
 \hline
 2 & 2 - 1 \\
 \hline
 & 1 - 0
 \end{array}$$

Ans:-

$(86)_{10}$ into binary is $(1010110)_2$

2. convert $(96.625)_{10}$ to binary.

$$\begin{array}{r|l}
 2 & 96 \\
 \hline
 2 & 48 - 0 \\
 \hline
 2 & 24 - 0 \\
 \hline
 2 & 12 - 0 \\
 \hline
 2 & 6 - 1 \\
 \hline
 2 & 3 - 1 \\
 \hline
 2 & 1 - 1 \\
 \hline
 & 0
 \end{array}$$

0.625

$$0.625 \times 2 = 1.250 \rightarrow 1$$

$$0.250 \times 2 = 0.500 \rightarrow 0$$

$$0.500 \times 2 = 1.000 \rightarrow 1$$

Ans:-

$(96.625)_{10}$ to binary is $(1011100.101)_2$

3. Convert $(10110101)_2$ into decimal

1	0	1	1	0	1	0	1	
								$1 \times 2^0 = 1$
								$0 \times 2^1 = 0$
								$1 \times 2^2 = 4$
								$0 \times 2^3 = 0$
								$1 \times 2^4 = 16$
								$1 \times 2^5 = 32$
								$0 \times 2^6 = 0$
								$1 \times 2^7 = 128$
								<u>181</u>

Ans:-

$(10110101)_2$ into decimal is $(181)_{10}$

4. $(111001.101)_2$ into decimal.

1	1	1	0	0	1	
						$1 \times 2^0 = 1$
						$0 \times 2^1 = 0$
						$0 \times 2^2 = 0$
						$1 \times 2^3 = 8$
						$1 \times 2^4 = 16$
						$1 \times 2^5 = 32$
						<u>57</u>

1	0	1	
			$1 \times 2^{-3} = 0.125$
			$0 \times 2^{-2} = 0$
			$1 \times 2^{-1} = 0.5$
			<u>0.625</u>

Ans:-

$(111001.101)_2$ into decimal is $(57.625)_{10}$

5. Convert $(572)_8$ into decimal

$$\begin{array}{r}
 5 \quad 7 \quad 2 \\
 \begin{array}{l}
 | \quad | \quad | \\
 \hline
 2 \times 8^0 = 2 \\
 7 \times 8^1 = 56 \\
 5 \times 8^2 = 320 \\
 \hline
 378
 \end{array}
 \end{array}$$

Ans :- $(572)_8$ into decimal
is $(378)_{10}$

6. Convert $(7C)_{16}$ into decimal

$$\begin{array}{r}
 7 \quad C \\
 \begin{array}{l}
 | \quad | \\
 \hline
 12 \times 16^0 = 12 \\
 7 \times 16^1 = 112 \\
 \hline
 124
 \end{array}
 \end{array}$$

Ans :- $(7C)_{16}$ into decimal is $(124)_{10}$

7. Convert $(11011101.101)_2$ into octal and hexadecimal.

Octal :-

$$\begin{array}{cccc}
 011 & 011 & 101 & .101 \\
 3 & 3 & 5 & .5
 \end{array}$$

Ans :-

(335.5)

Hexadecimal :-

$$\begin{array}{cccc}
 1101 & 1101 & .1010 \\
 13 & 13 & .10 & \rightarrow DD.A
 \end{array}$$

Ans :- $DD.A$

$(11011101.101)_2$ into octal and hexadecimal is
 (335.5) and $(DD.A)$

8. find the 1's and 2's complement of 11010101 .

1's complement $\rightarrow 11010101 \rightarrow 1s \rightarrow 00101010$

2's complement $\rightarrow 11010101 \rightarrow 1s \rightarrow 00101010$

$$\begin{array}{r} 1 \\ 00101010 \\ \hline 00101011 \end{array}$$

1's complement $\rightarrow 00101010$

2's complement $\rightarrow 00101011$

9. subtract $(110101)_2 - (011011)_2$ using 2's complement

$A \rightarrow 110101$

$B \rightarrow 011011$

$$\begin{array}{r} 100100 \\ \hline 100101 \end{array}$$

$$\begin{array}{r} 110101 \\ 100101 \\ \hline 1011010 \end{array}$$

Ans:-

$(011010)_2$

10. find the 9's and 10's complement of 4837 .

9's complement $\rightarrow 9-4, 9-8, 9-3, 9-7$

5 1 6 2 $\rightarrow 5162$

10's complement $\rightarrow 9-4, 9-8, 9-3, 9-7$ and Add 1

$$\begin{array}{r} 5162 \\ \hline 5163 \end{array} \rightarrow 5163$$

the 9's and 10's complement is 5162, 5163.

11. Represent -47 using 8-bit sign magnitude, 1's complement and 2's complement.

Sign magnitude :-

$$\begin{array}{r} -47 \quad 2 \quad 47 \\ \hline 2 \quad 23 \quad -1 \\ \hline 2 \quad 11 \quad -1 \\ \hline 2 \quad 5 \quad -1 \\ \hline 2 \quad 2 \quad -1 \\ \hline 1 \quad -0 \end{array}$$

101111 change into 8 bit

Ans:- 10101111

1's complement $\rightarrow$

00101111 change into 1's complement is
11010000

2's complement $\rightarrow$

$$\begin{array}{r} 11010000 \rightarrow 11010000 \\ \hline 11010001 \end{array}$$

sign magnitude $\rightarrow$ 10101111

1's complement $\rightarrow$ 11010000

2's complement $\rightarrow$ 11010001

12. Convert Decimal 73 into BCD.

$$7 \rightarrow 0111$$

$$3 \rightarrow 0011$$

Ans:-

$$01110011 \rightarrow \text{BCD}$$

13. Convert Decimal 96 into Excess-3.

$$9 \rightarrow 1100$$

$$9 \rightarrow \begin{array}{r} 1001 \\ 0011 \rightarrow 3 \\ \hline 1100 \end{array}$$

$$6 \rightarrow \begin{array}{r} 0110 \\ 0011 \rightarrow 3 \\ \hline 1001 \end{array}$$

$$6 \rightarrow 1001$$

Ans:-

$$11001001$$

14. Convert Binary into Gray code $\rightarrow 1010111$

$$1 \rightarrow 0 \rightarrow 1 \rightarrow 0 \rightarrow 1 \rightarrow 1 \rightarrow 1$$

↓

$$1 \ 1 \ 1 \ 1 \ 1 \ 0 \ 0$$

Ans:-

$(1010111)_2$ into Gray code is 111100

15. Convert Gray code into binary $\rightarrow 10110110$

$$\begin{array}{cccccccc} 1 & 0 & 1 & 1 & 0 & 1 & 1 & 0 \\ \downarrow & \nearrow & \downarrow & \nearrow & \downarrow & \nearrow & \downarrow & \nearrow \\ 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 \end{array}$$

Ans:-

10110110 Gray code into binary is 11011011

16. simplify using Boolean Laws:-

a) $AB + A\bar{B} + \bar{A}C$

$$F = AB + A\bar{B} + \bar{A}C$$

$$F = A(B + \bar{B}) + \bar{A}C$$

$$F = A(1) + \bar{A}C$$

$$F = A + \bar{A}C$$

Apply Absorption law

$$A + \bar{A}C = A + C$$

Ans :- $A + C$

b) $A + A\bar{B} + \bar{A}BC$

$$F = A + A\bar{B} + \bar{A}BC$$

Apply absorption law.

$$A + A\bar{B} = A$$

so $\rightarrow A + \bar{A}BC$

$$A + \bar{A}BC = A + BC$$

$$\therefore A + BC$$

Ans :- $A + BC$

17. Convert truth table to sop and pos form.

A	B	Y
0	0	1
0	1	1
1	0	0
1	1	0

Sop :-

A	B	Y	pos
0	0	1	$\bar{A}\bar{B}$
0	1	1	$\bar{A}B$
1	0	0	$A\bar{B}$
1	1	0	AB

$$Y = \bar{A}\bar{B} + \bar{A}B$$

pos :-

A	B	Y	sop
0	0	1	$A+B$
0	1	1	$A+\bar{B}$
1	0	0	$\bar{A}+B$
1	1	0	$\bar{A}+\bar{B}$

$$Y = (\bar{A} + B) \cdot (\bar{A} + \bar{B})$$

18. simplify using K-maps: $F(A, B) = \Sigma(1, 2, 3)$.

A \ B	$\bar{B}$	B
$\bar{A}$	0	1
A	1	1

$F(A, B)$ pair 1 = B

pair 2 = A

$$F(A, B) = A + B$$

Ans :-

$$F(A, B) = A + B$$

19. simplify using K-Maps and draw logic circuits

$$F(A, B, C) = \Sigma(1, 2, 3, 5, 7)$$

A \ BC	$\bar{B}\bar{C}$	$\bar{B}C$	$B\bar{C}$	BC
$\bar{A}$	0	1	1	1
A	0	1	1	0

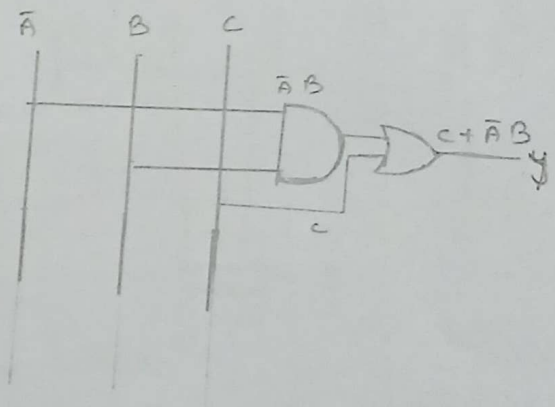
Quad = C

pair = $\bar{A}B$

Ans :-

$$F(A, B, C) = C + \bar{A}B$$

logic circuit :-



Qo. simplify using K-Maps and draw logic circuit?

a) $F(A, B, C, D) = \Sigma (0, 1, 2, 5, 7, 8, 9, 10, 13, 15)$

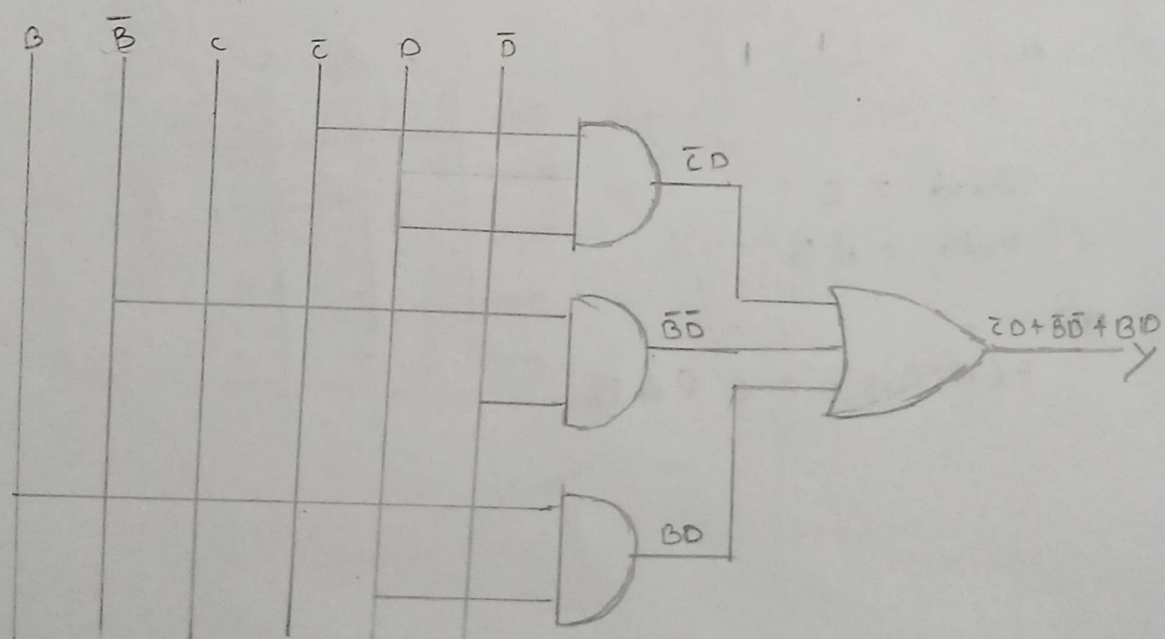
AB \ CD	$\bar{C}\bar{D}$	$\bar{C}D$	CD	$C\bar{D}$
$\bar{A}\bar{B}$	1	1		1
$\bar{A}B$		1	1	
AB		1	1	
$A\bar{B}$	1	1		1

Octus $\neq$ Quad 1 = $\bar{C}D$

Quad 2 = $\bar{B}\bar{D}$

Quad 3 = BD

$F(A, B, C, D) = \bar{C}D + \bar{B}\bar{D} + BD$



Q0. b) $F(w, x, y, z) = \sum (1, 3, 4, 5, 7, 9, 13, 15)$

$w \backslash x \backslash yz$	$\bar{y}z$	$\bar{y}\bar{z}$	$y\bar{z}$	yz
$\bar{w}\bar{x}$		1	1	
$\bar{w}x$	1	1	1	
$w\bar{x}$		1	1	
wx		1		

Quad 1 = $\bar{y}z$

Quad 2 = xz

pair 1 = $\bar{w}\bar{x}z$

pair 2 = $\bar{w}x\bar{y}$

$F(w, x, y, z) = \bar{y}z + xz + \bar{w}\bar{x}z + \bar{w}x\bar{y}$

